### Worldwide Spreading of Economic Crises

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## MODEL

- view the world as a network of all countries
- each country is a node ~ 200 nodes
- connection between nodes: economic relations
- fully connected network?
  answer = no
- all connections are one-way, with specific weight
- k-shell decomposition method to rank countries
- start a crisis on a single node
- allow the crisis to propagate throughout the network
- use simple propagation model, e.g. SIR model
- monitor countries that are affected

## DATA

• CON (Corporate Ownership Network):

4000 world corporations with the highest turnover with 616000 direct or indirect subsidiaries: network of 206 countries

 ITN (International Trade Network):
 Detailed information about international trade (import-export) between 82 countries

#### **CON** network

• Total link weight

$$w_{tot}^{(ij)} = w_{ij} + w_{ji}$$

• Total node weight

$$\widetilde{w}_{tot}^{i} = \sum_{j} w_{ij} + \sum_{j} w_{ji}$$



### GDP vs Weight

- total node weight of a node  $i \ \widetilde{w}_{tot}^i = \sum_j w_{ij} + \sum_j w_{ji}$ versus its GDP
- linear relation:
  Nodes with high GDP have high weight



#### The k-shell decomposition method

- Start with the actual network
- Identify all nodes that have k=1, and remove them.
- Repeat until we are left only with nodes that have k>=2
- These nodes constitute the shell  $k_s=1$
- Similarly remove all nodes with k=2, in order to find the nodes with k<sub>s</sub>=2, etc.

# Illustration of the layered structure of the network



The core shown is the actual core obtained for CON

# Identifying the core using k-shell decomposition

- We need a cut-off parameter for the weights of the network in order to identify the most internal core.
- We choose one that leads to a stable core



#### Change in the k-shell ranking

 Most countries (82%) are located in almost the same distance from the nucleus for both CON and ITN



#### Cores

#### • CON:

USA (US) United Kingdom (GB) France (FR) Germany (DE) Netherlands (NL) Japan (JP) Sweden (SE) Italy (IT) Switzerland (CH) Spain (ES) **Belgium (BE)** Luxembourg (LU)

ITN: USA (US) United Kingdom (GB) France (FR) Germany (DE) Netherlands (NL) Japan (JP) Italy (IT) Spain (ES) Belgium (BE) Luxembourg (LU) China (CN) Russia (RU)



#### k-shell ranking of countries



### The SIR model

- SIR (Susceptible, Infected, Removed),
- q=probability of infection
- Initially all nodes are susceptible (S)
- Then, a random node is infected (I)
- virus is spread in the network, all "I" nodes become "R"
- This process continues until the virus either
  - has been spread in the entire network, or
  - has been totally eliminated
- M=infected mass
- Duration



### Modeling crisis spreading: SIR

- Infection probability:  $p_{ij} \propto m \cdot w_{tot}^{(ij)} / \tilde{w}_{tot}^{j}$
- w<sup>(ij)</sup><sub>tot</sub>/w<sup>j</sup><sub>tot</sub>: the economic dependence of country "j" on country "i"
- m : the strength of a crisis

# Infection depends on the shell where the crisis originates



Infected Fraction

#### k-shell ranking of countries



### Determining if infected or not:

- Perform 1000 realizations of SIR
- Use arbitrary range
  - 0- 200: not infected
  - 200-800: can not tell
  - 800-1000: infected

#### • If crisis starts in nucleus (inner core)

- 90.6% of countries infected
- 96.6% worst case scenario
- If crisis starts shell k=6
  - 3.3% of countries infected
  - 18.9% worst case scenario

# Countries affected by the 2008 economic crisis



# Model results: a crisis starts in US and spreads through CON



#### Example: Belgium

- 29<sup>th</sup> in the world in GDP
- Start a crisis with m=4.5
- Will affect 60% of world (average of 50 runs)
- Worst case senario: maximum value of the same 50 runs. Will affect 95% of world

#### Conclusions

- Spreading of a crisis
- we used a NETWORK approach
- we used real data (companies, impo-expo)
- k-shell decomposition method
- SIR spreading mechanism
- a small number of countries (12) is critical
- not necessarily the largest economies







#### Contributed to this work:

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- Shlomo Havlin (Bar-Ilan, Israel)
- Celine Rozenblat, Lausanne, Switzerland
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