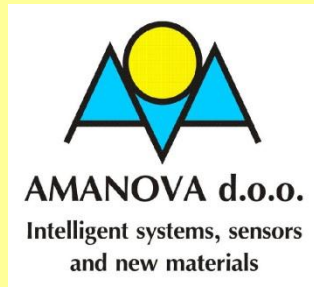


# FORECASTING DEVELOPMENT OF TRAFFIC JAM AT A HIGH-WAY BOTTLENECK

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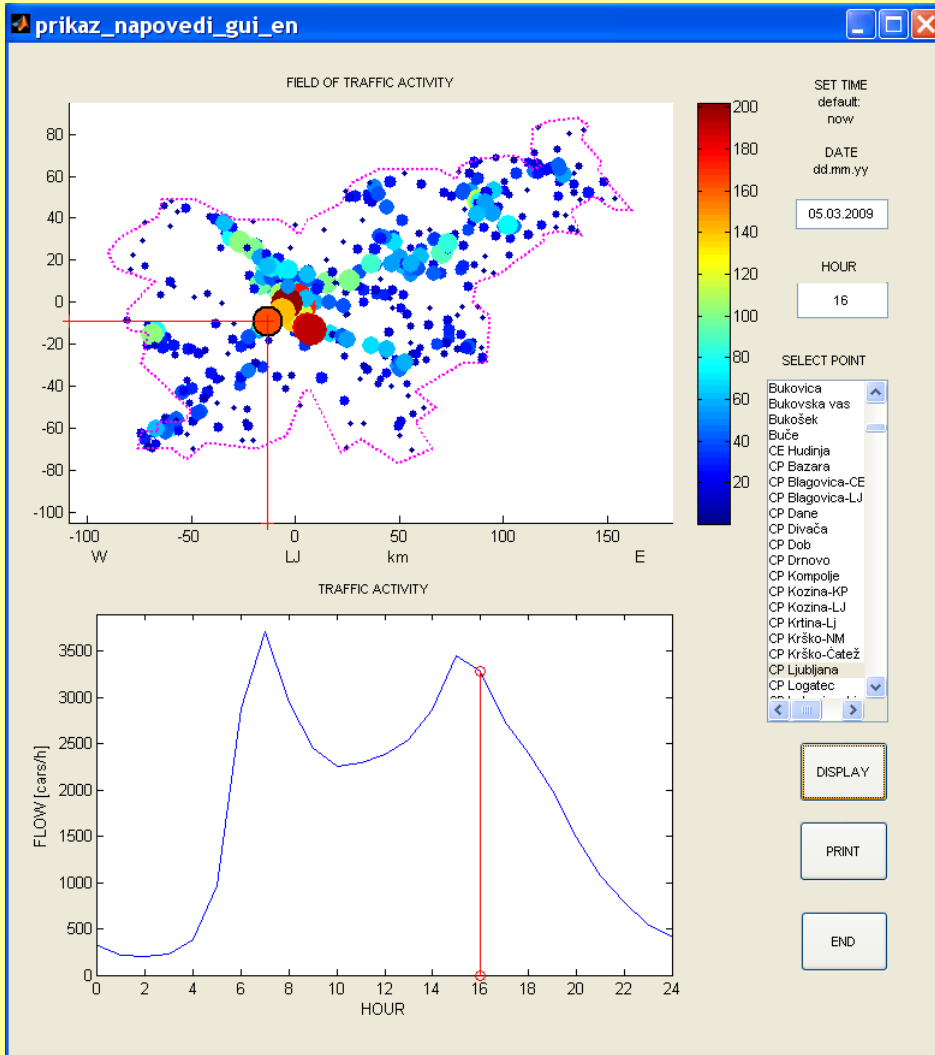
# Objectives

- **Problem:** How to forecast development of a traffic jam at a bottleneck of high-way?
- **Source of information:** Predicted traffic flow rate at a selected road section.
- **Mathematical tool:** Coupled fundamental traffic flow diagram and continuity equation.
- **Goal:** To develop a new tool for traffic information center.

# Prediction of traffic flow rate

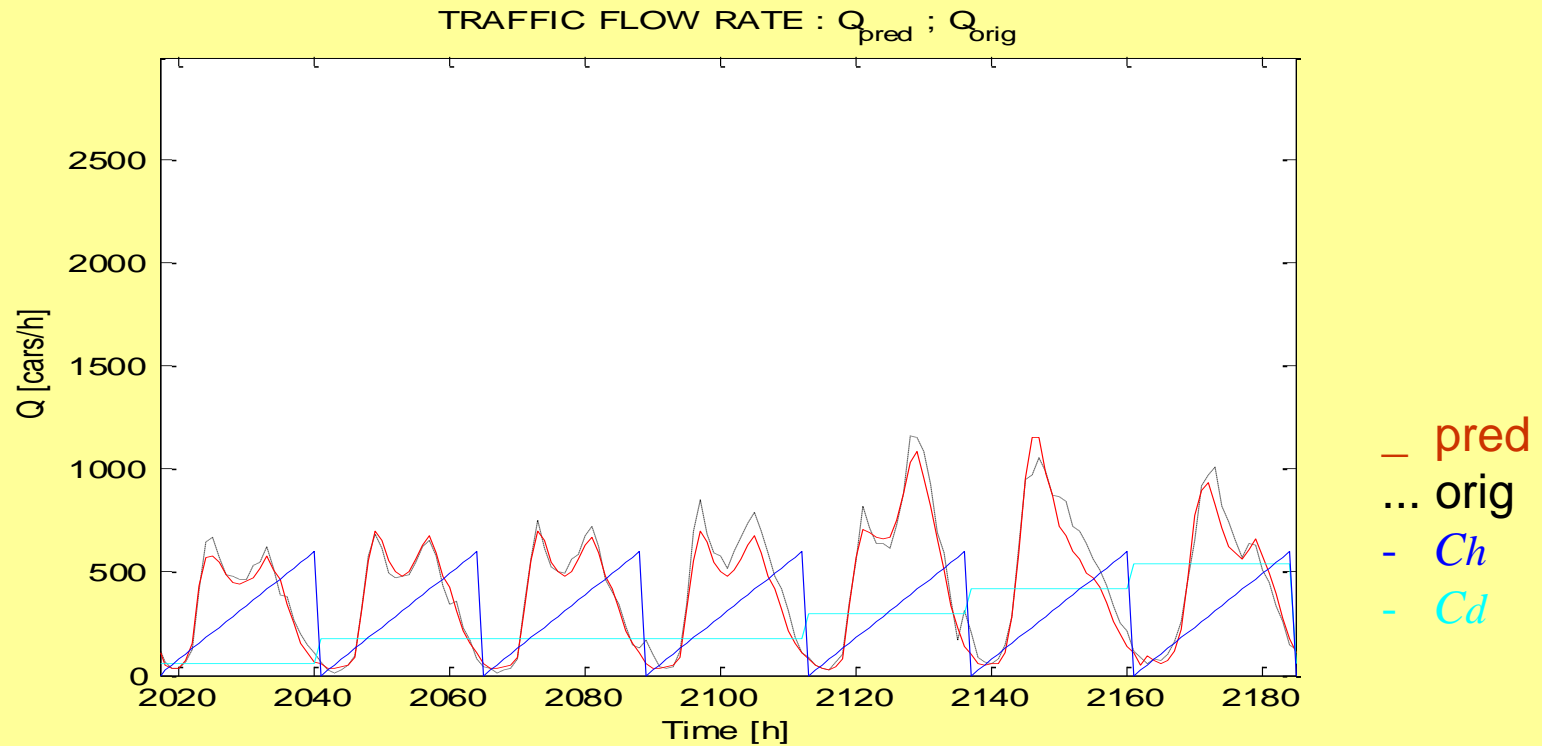
- **Basis:** Prediction of traffic activity on high-ways of Slovenia is performed by a non-parametric statistical model using previously recorded time series of flow rate.
- **Applicable tool:** The model operates in the graphic user interface that yields time series of the predicted flow rate at a selected time interval and road sector.
- **Goal of the next step:** To develop a model for mapping of the forecast traffic flow into predictor of the traffic jam length at the bottleneck.

# Graphic user interface for prediction of traffic flow rate



- For a prediction the user sets:
- **day, hour, and point**
- The interface displays:
- Top: **field of traffic activity**
- Bottom: **traffic flow rate**
- Lines: selected place and hour

# Example of a prediction

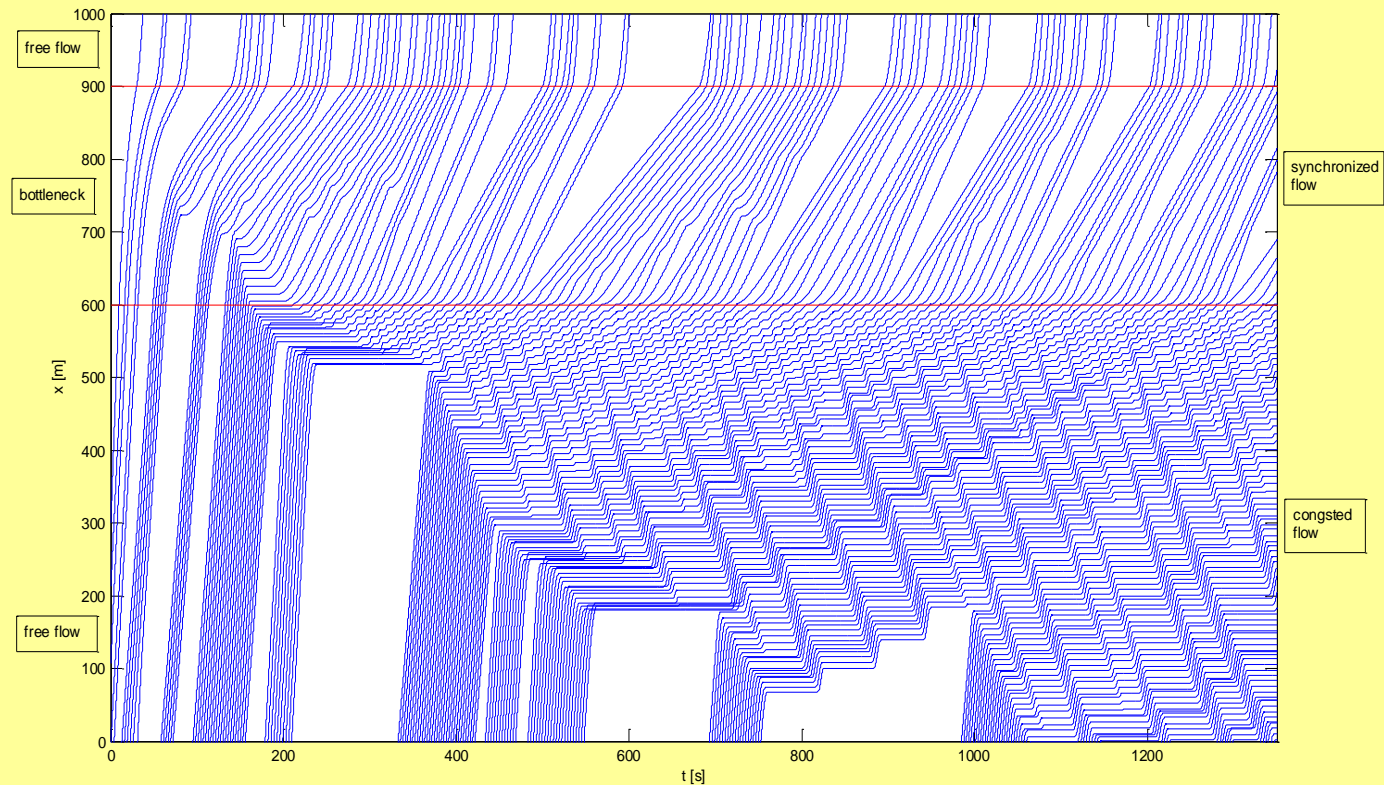


Correlation coefficient of predicted and observed flow rate is ~97%

# Micro-dynamic modelling of jam evolution at a bottleneck

Micro-dynamic model stems from driving rules and predictor of traffic flow.

Micro-model is not convenient for application.



The goal: Macro-modeling based on fundamental diagram of flow and continuity equation. Boundary condition is determined by the predicted flow

# Variables

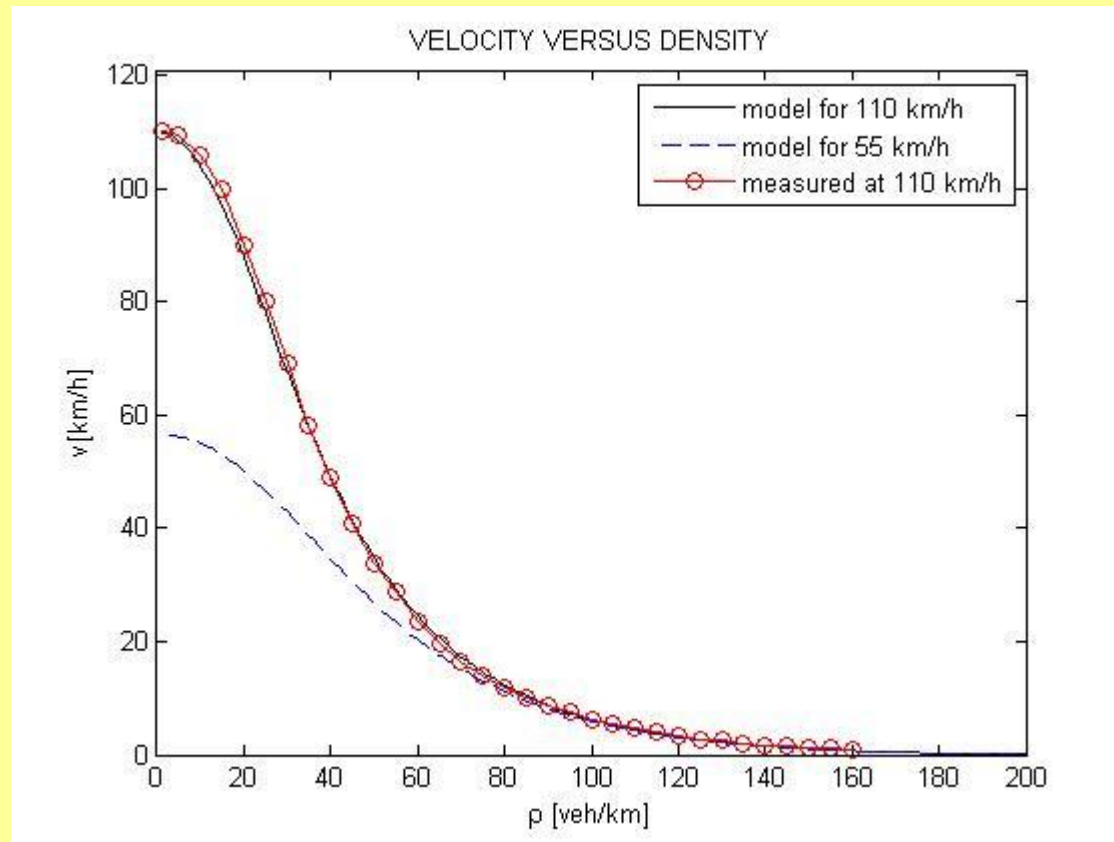
- **Basic variables:**
  - $r$  : distance between cars,  $\rho=1/r$  : density of cars
  - $v$  : mean velocity,
  - $v_e(\rho)$  : equilibrium velocity
  - $Q=\rho v$  : flow rate
- **Parameters and reference variables:**
  - $\lambda \sim 5\text{m}$  : car length,  $r - \lambda$  : clear spacing
  - $\tau \sim 1\text{s}$  : reaction time
  - $u = C \lambda / \tau$  : characteristic velocity;  $C \sim 3$
  - $r = \lambda + \tau w$  : proper distance
  - $w = (r - \lambda) / \tau$  : proper velocity

# Equilibrium velocity

- Equilibrium velocity  $v_e$  is determined by the velocity limit  $v_o$  and the proper velocity  $w$ . Constraints:  $v_e \leq v_o$  and  $v_e \leq w$  lead to
- **Joint constraint:**  $\frac{1}{v_e} = \frac{1}{v_o} + \frac{A}{w}$
- The proper weight:  $A = \frac{3\lambda}{r-\lambda} = \frac{u}{w}$  yields
- **The fundamental law:**  $v_e = \frac{v_o}{1 + \frac{uv_o}{w^2}}$

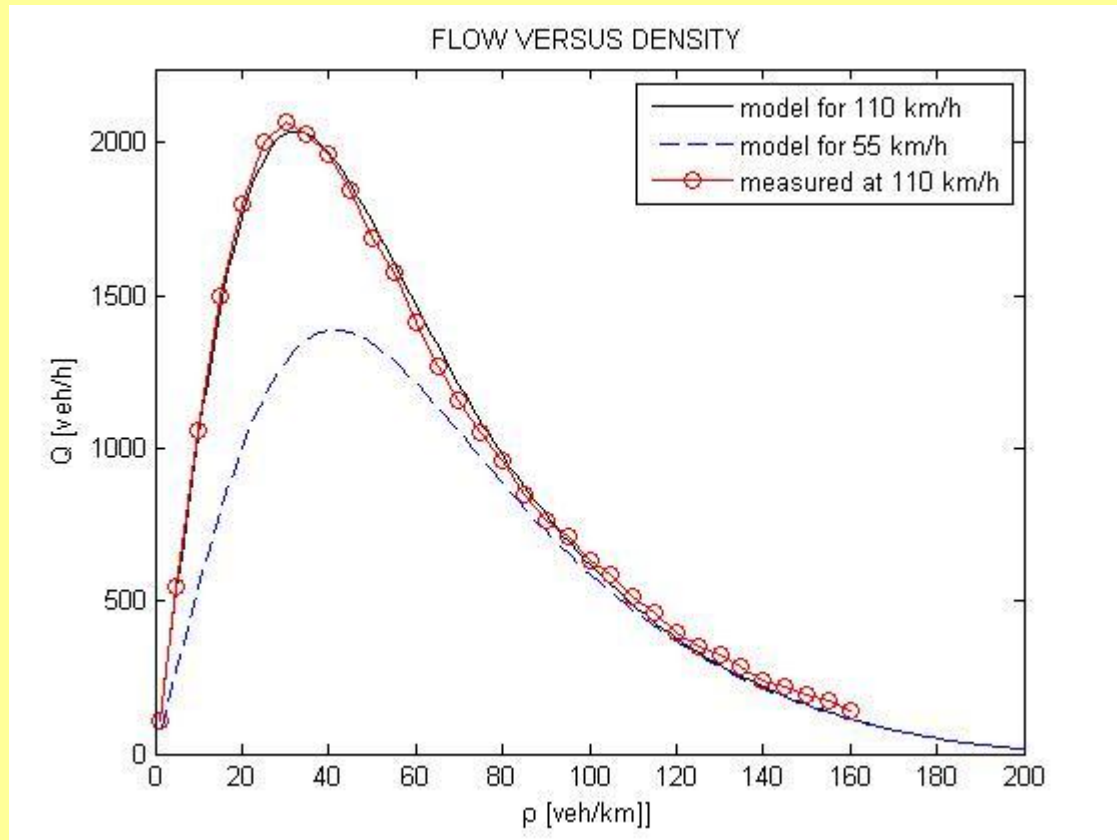


# Fundamental diagram $v_e(\rho)$



Dependence of equilibrium velocity  $v_e$  on the density  $\rho$ .  
Measured data from: D. Helbing: Verkehrsdynamik

# Fundamental diagram $Q(\rho)$



Dependence of the flow rate  $Q$  on the density  $\rho$ .

# Field equations

- Velocity adaptation law:

- $$\frac{\partial v}{\partial t} + v \frac{\partial v}{\partial x} = \frac{v_e(\rho) - v}{T} ;$$

- Relaxation time:  $T \cong 3\tau$

- Continuity equation:

- $$\frac{\partial \rho}{\partial t} + \frac{\partial \rho v}{\partial x} = I(x, t)$$

- Traffic source term:

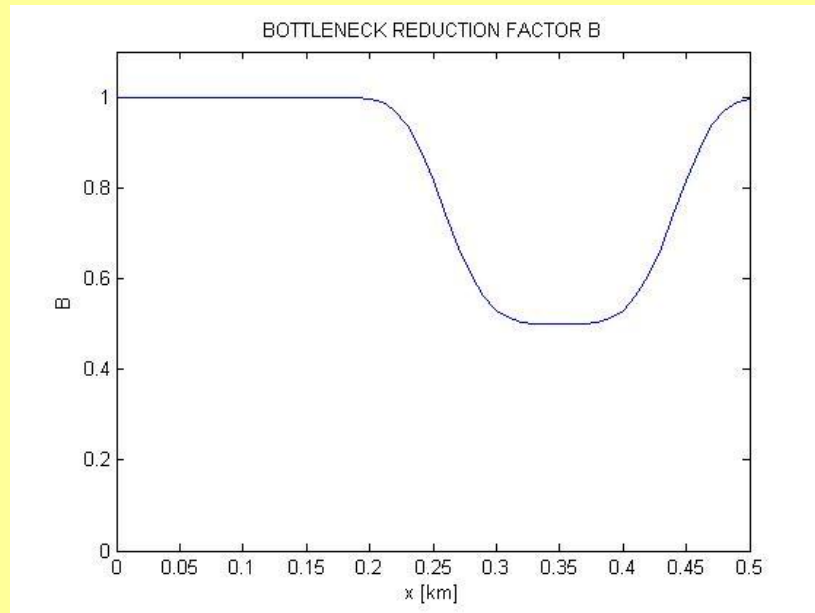
- $I(x, t) = Q(t)\delta(x, t) \quad ; \quad Q(t) \text{ is forecast}$

# Numerical treatment

- Cell dimensions:  $\Delta x = \lambda$  ;  $\Delta t = 0.1\tau$
- Intervals:  $0 < x < 0.5\text{km}$  ;  $0 < t < 1\text{h}$
- Initial and boundary conditions:  
 $\rho = 0$  ;  $v = 0$ .
- Source term specified by the predicted flow rate  $Q$  centered at rush hour:  $t = 0.5\text{h}$ .
- Transition to non-dimensional variables:  
 $t/\tau$  ;  $x/\lambda$  ;  $v \tau/\lambda$  ;  $\rho \lambda$  ;  $Q\tau$

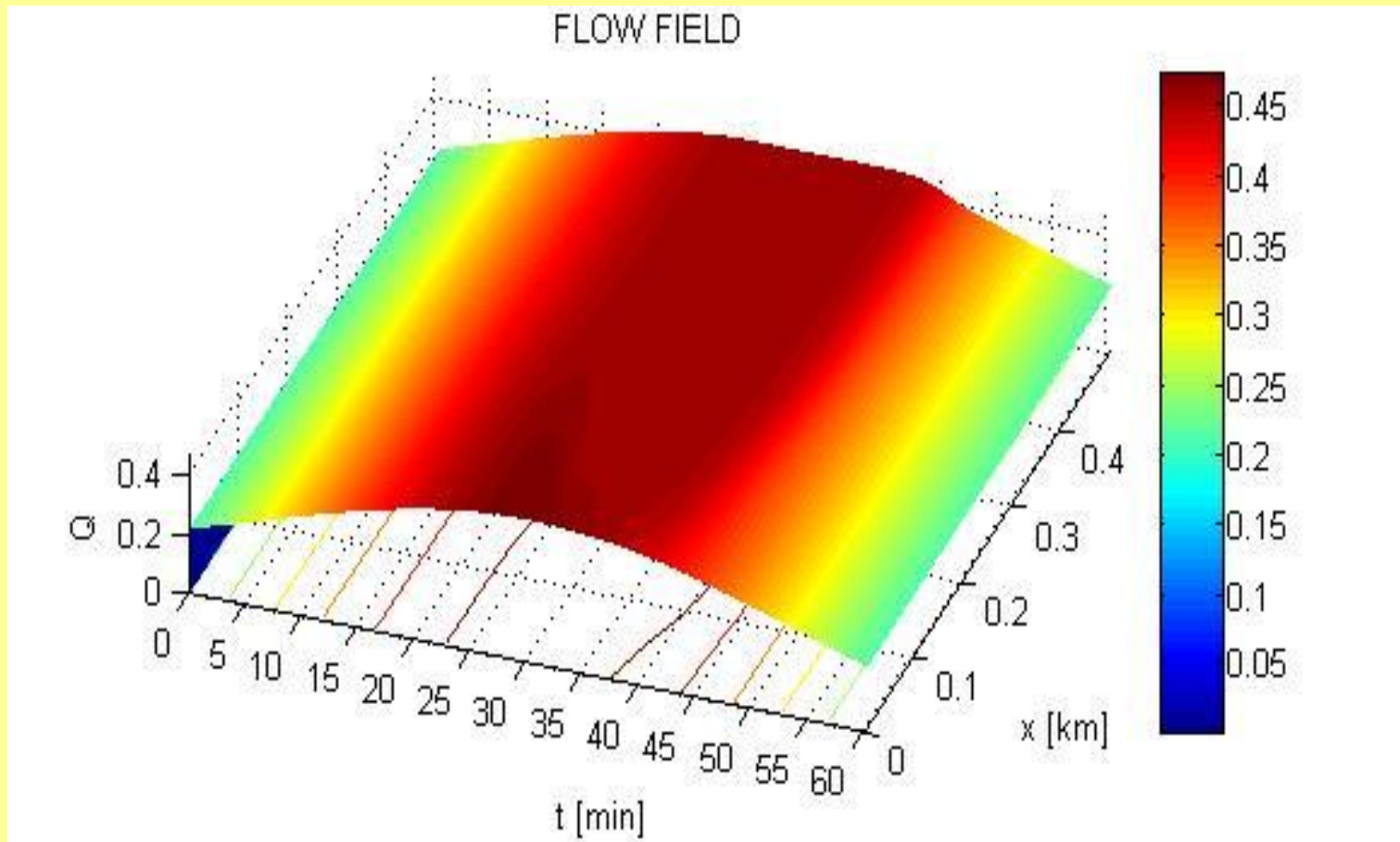
# Specification of the bottleneck

- Position:  $0.2\text{km} < x < 0.4\text{km}$
- Reduced speed:  $0.5 v_0$



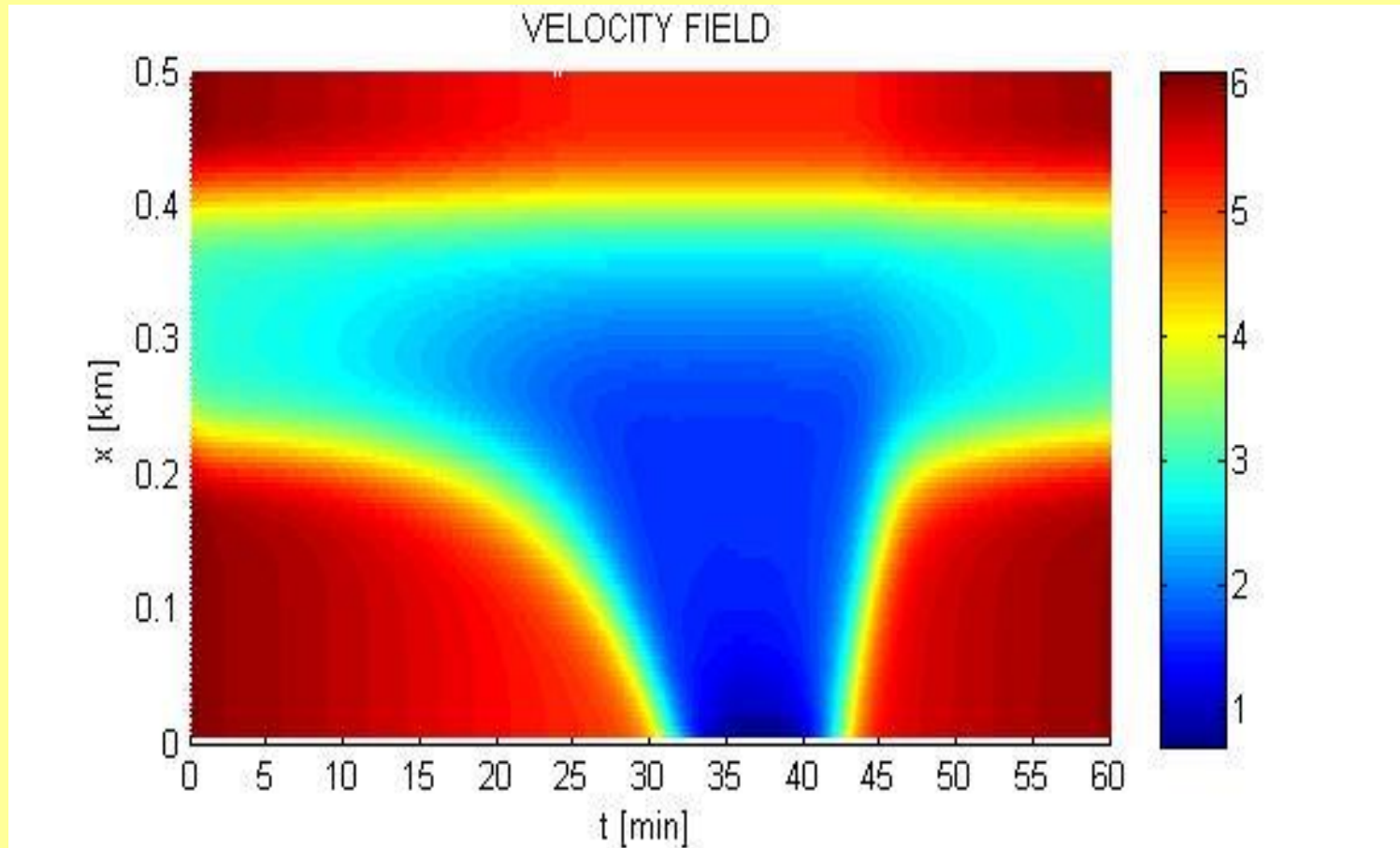
Dependence of the velocity reduction factor  $B$  on  $x$ .

# Flow field – $Q(x, t)$



Parameters:  $v_o=110\text{km/h}$  ;  $Q_{max}=1700\text{ veh/h}$

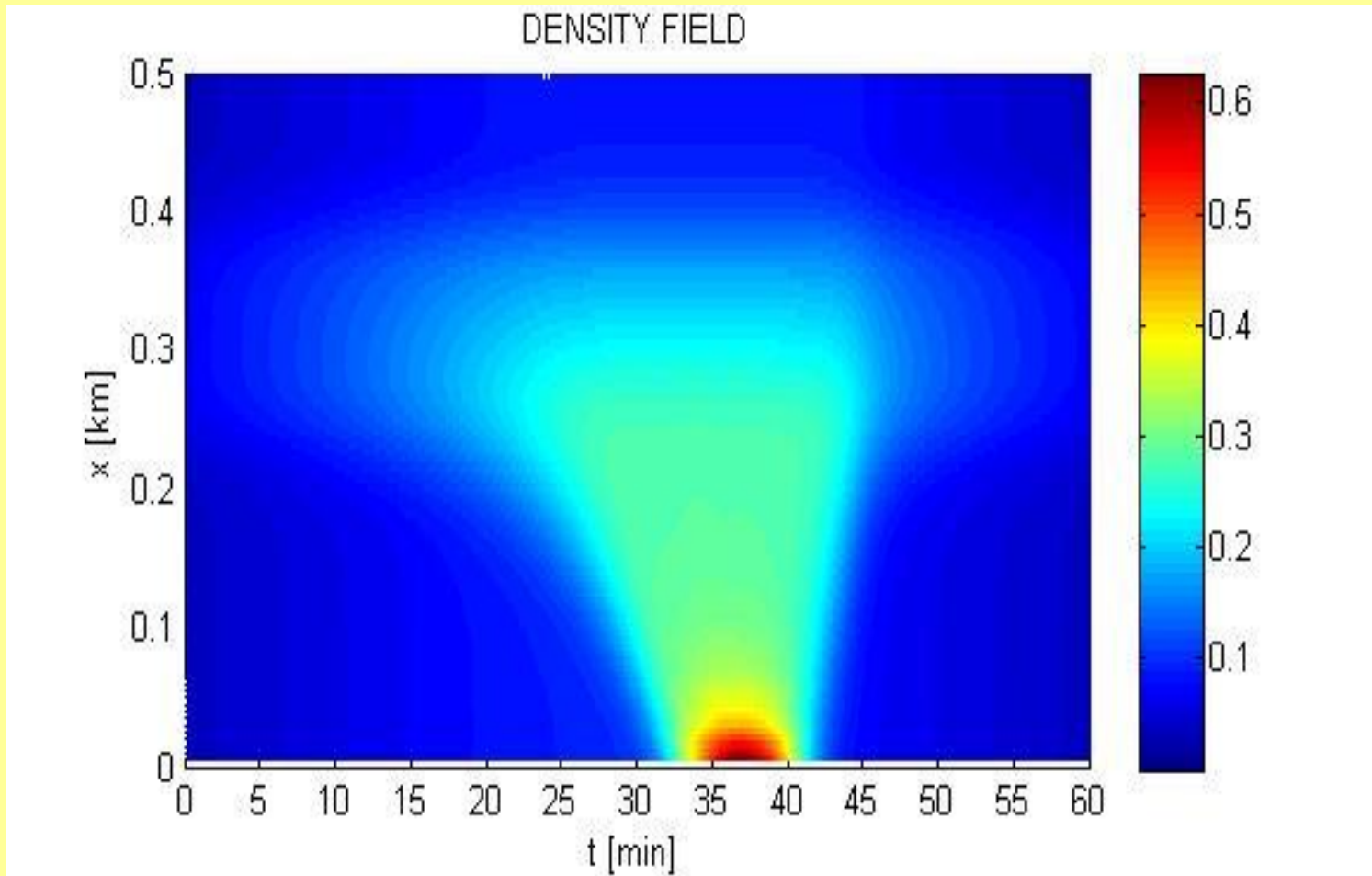
# Velocity field – $v(x, t)$



Parameters:  $v_o=110\text{km/h}$  ;  $Q_{max}=1700\text{ veh/h}$

Backward jam propagation velocity:  $v_{jam} \sim -0.2\text{km}/10\text{min}$

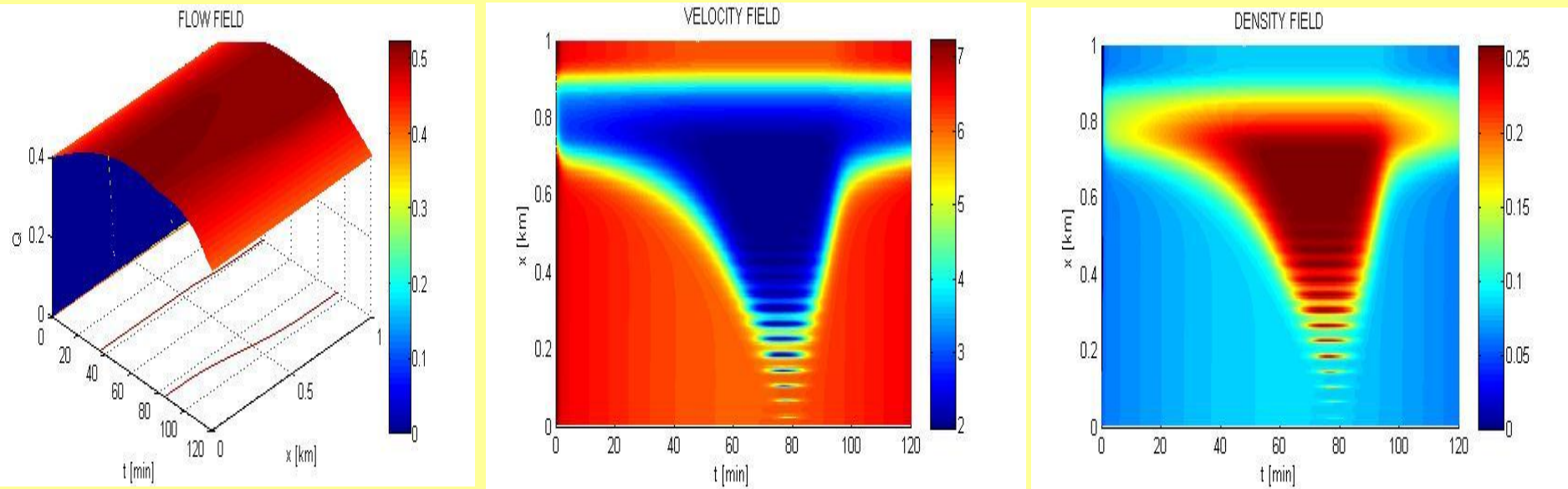
# Density field – $\rho(x, t)$



Parameters:  $v_o=110\text{km/h}$  ;  $Q_{max}=1700\text{ veh/h}$



# Field distributions



Parameters:  $v_o=130$  km/h ;  $Q_{max}=1875$  veh/h

# Application of jam forecasting

**Observation:** The evolution of traffic jam at the bottleneck critically depends on the input flow. Forecasting of its length is possible based upon the predicted flow.

**Benefit:** Before installing a bottleneck one can estimate its influence and diminish disturbances by a proper adaptation of the bottleneck structure.

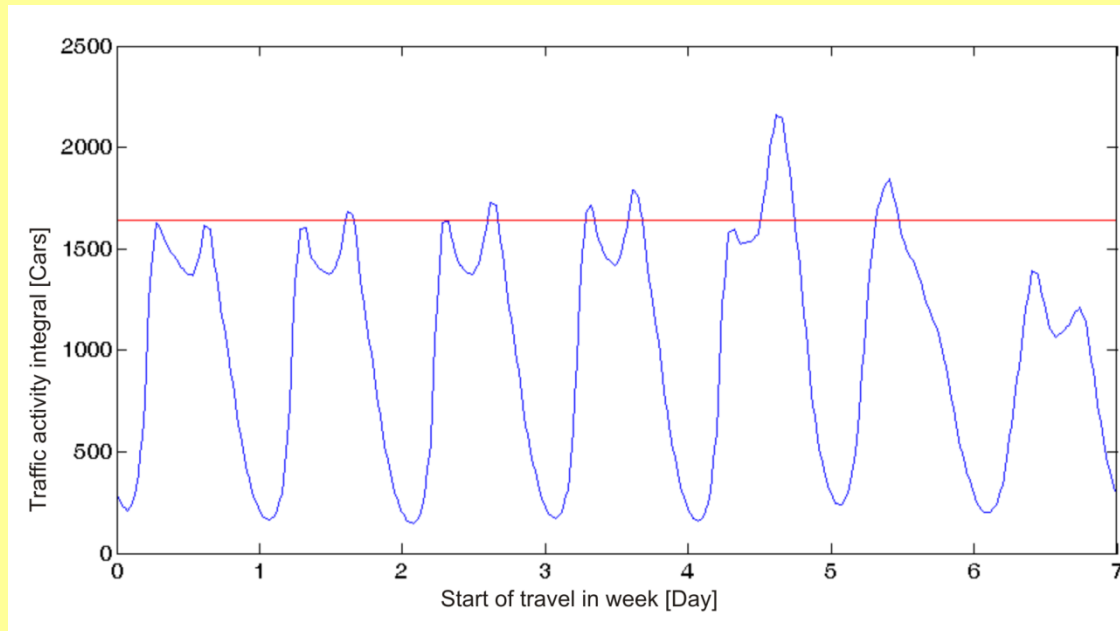
# Conclusions

- Fundamental traffic law and continuity equation describe the evolution of a jam at the bottleneck.
- Forecasting provides support for traffic information center and road services.
- The next step is to transfer predicted data to drivers over mobile telephones.

# References

1. I. Grabec, F. Švegl, *Modeling and Forecasting of Traffic Flow*, Proc. ISEP 2010, Ljubljana, March 29-30, 2010
2. F. Švegl, I. Grabec, *Prediction of winter driving conditions*, Proc. of the **International Road Weather Conference - SIRWEC – 15<sup>th</sup>**, Quebec, CA, February 5-7, 2010
3. D. Helbing, *Verkehrsdynamik*, **Springer** (Berlin, 1997)
4. This research was supported by the company **DARS**

# Forecasting of kritical traffic load on a way from KP to MB



**Blue** – integral of traffic flow from Koper to Maribor

**Red** – road capacity

**Intersection** – congestions start to develop