

# Basics of Renewable Energy Forecasting

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Through this lecture and additional study material, it is aimed for the students to be able to:

- ❶ Describe the **different types of renewable energy forecasts**, in plain words and in a more mathematical manner
- ❷ Explain why using such or such forecasts for **different type of decision-making problems**
- ❸ Discuss the origins and characteristics of **forecast uncertainty**

## Wind Energy

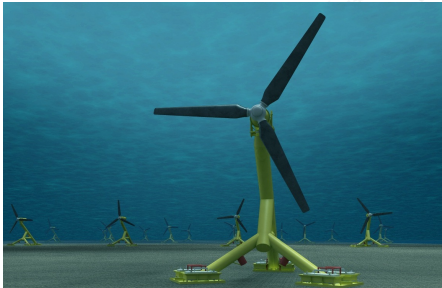


## Wave Energy (could be)

*... Also nothing on **Solar Energy** today, though all concepts are similar.*

And for another time...!

*These actually are tidal energy converters*



*Do you know what these are?*

## ① Forecast: why and in what form?

- forecasting in electricity markets
- the case of renewable energy forecasts
- forecasts as input to decision-making problems
- benefits from considering uncertainty

## ② Uncertainty origins and basic characteristics

- origins of uncertainty: weather forecasts, power curves, etc.
- basic characteristics

## ③ From deterministic to probabilistic forecasts

- what a deterministic forecast really is...
- illustration of forecast types: point, quantile, intervals, densities, trajectories

## 1 Forecast: why and in what form?

- Forecasting is a *natural first step* to decision-making
- Believing we know what will happen
  - helps making decisions
  - but mainly, makes us more confident about it!
- Key application areas include:
  - weather and climate
  - economics and finance
  - logistics
  - insurance, etc.

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"But to be fair, there's a fifty percent chance of just about anything."



- Different actors may have different needs...
  - market participant, **supply side** (e.g., conventional generator, wind farm operator)
  - market participant, **demand side** (e.g., retailer)
  - participants in neighboring markets
  - **market operator**
  - **system operator**
  - but also, *you and I*



- Different actors may have different needs...
  - market participant, **supply side** (e.g., conventional generator, wind farm operator)
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  - participants in neighboring markets
  - **market operator**
  - **system operator**
  - but also, *you and I*
- One may want forecasts for:
  - the *electric load*
  - *day-ahead prices*
  - potential *imbalance sign*
  - *regulation prices/penalties*
  - potential *congestion on interconnectors*
  - etc.
  - *Generation from renewable energy sources!!!*
- **Nearly all these quantities are driven by weather and climate!**

- Forecast information is widely used as input to several decision-making problems:
  - definition of **reserve** requirements (i.e., backup capacity for the system operator)
  - **unit commitment** and **economic dispatch** (i.e., least costs usage of all available units)
  - coordination of renewables with **storage**
  - design of optimal **trading** strategies
  - electricity **market-clearing**
  - optimal **maintenance planning** (especially for offshore wind farms)
- Inputs to these methods are:
  - deterministic forecasts
  - probabilistic forecasts as **quantiles, intervals, and predictive distributions**
  - probabilistic forecasts in the form of **trajectories** (/scenarios)
  - **risk indices** (broad audience applications)
- For nearly all of these problems, optimal decisions can only be obtained if fully considering forecast uncertainty...

## A recommended book

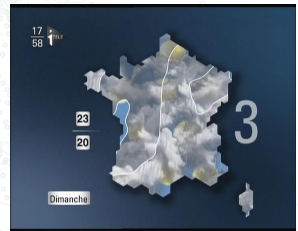
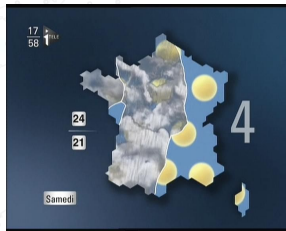
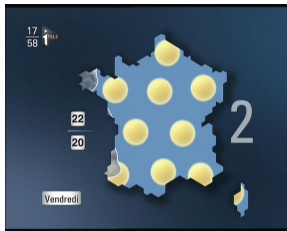
S. Makridakis, R. Hogarth, A. Gaba

### **Dance with Chance: Making Luck Work for You**



# The problem with forecast uncertainty estimation

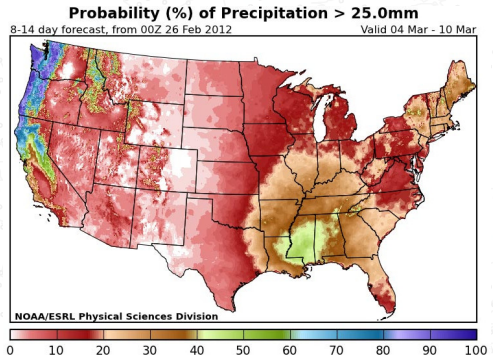
- The French National meteorological office (Meteo-France) has been communicating “*confidence indices*” (indices de confiance) along with their forecasts for quite a while...
- Example set of forecasts: (from “1 = low confidence” to “5 = high confidence”)



- *Do you get something out of it?*

## Now... the “big mouth” paradox

- It might always be difficult to trust someone providing you with forecasts
- Even more so if these are probabilistic...
- Let us consider a simple american setup (focus on **New Orleans**), with two rival forecasters:
- The two competing forecasters tell you that:
  - **Forecaster A:**  
*It will rain next Monday, and the precipitation amount will be of 22mm*
  - **Forecaster B:**  
*There is a probability of 38% that precipitation is more than 25mm next week*
- Who would you hire?



[Extra reading: S Joslyn, L Nadav-Greenberg, RM Nichols (2009) Probability of precipitation: Assessment and enhancement of end-user understanding. *Bulletin of the American Meteorological Society* 90: 185–193 ([pdf](#))  
UR Karmarkar, ZL Tormala (2010). Believe me - I have no idea what I'm talking about: The effects of source certainty on consumer involvement and persuasion. *Journal of Consumer Research* 36(6): 1033–1049 ([pdf](#))]

## Example use of forecasts: market participation

- **Dutch electricity market** over the year 2002:
  - day-ahead market APX
  - regulation mechanism managed by TenneT, the TSO for the Netherlands
- Participation of a **15 MW wind farm**, without any storage device and without any control on the power production
- **Point** and **probabilistic** predictions (full predictive distributions) generated with state-of-the-art statistical methods
- **Revenue-maximization** strategies
  - based on point predictions only (persistence or advanced method)
  - derived from probabilistic predictions and a model of the participant's sensitivity to regulation costs

## Trading results

	Pers.	Adv. point pred.	Prob. pred.	Perfect pred.
Contracted energy (GWh)	44.37	45.49	62.37	46.41
Surplus (GWh)	18.12	9.87	4.89	0
Shortage (GWh)	16.08	8.95	20.85	0
Down-regulation costs ( $10^3$ €)	195.72	119.99	42.61	0
Up-regulation costs ( $10^3$ €)	79.59	52.01	61.46	0
Total revenue ( $10^3$ €)	1041.38	1145.69	1212.61	1317.69
Av. down-reg. unit cost (€/MWh)	10.80	12.15	8.71	0
Av. up-reg. unit cost (€/MWh)	4.95	5.81	2.95	0
Av. reg. unit cost (€/MWh)	8.05	9.13	4.04	0
<b>Av. energy price (€/MWh)</b>	<b>22.44</b>	<b>24.68</b>	<b>26.13</b>	<b>28.37</b>
<b>Part of imbalance (% prod. energy)</b>	<b>73.69</b>	<b>40.55</b>	<b>55.46</b>	<b>0</b>
<b>Performance ratio (%)</b>	<b>79.1</b>	<b>86.99</b>	<b>92.1</b>	<b>100</b>

[Source: P Pinson, C Chevallier, G Kariniotakis. Trading wind generation from short-term probabilistic forecasts of wind power. *IEEE Trans. on Power Systems* 22(3): 1148-1156 ([pdf](#))]

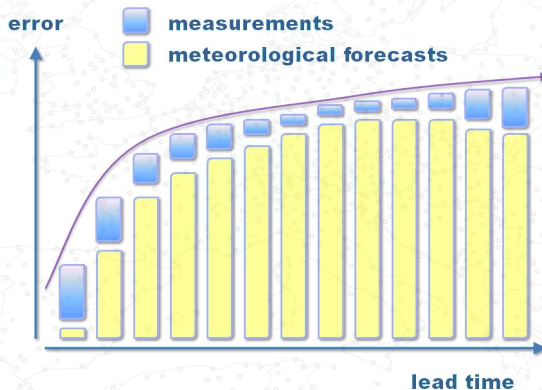
## 2 Uncertainty origins and basics



- To generate renewable energy forecasts in electricity markets, necessary inputs include:
  - recent power generation measurements
  - weather forecasts for the coming period
  - possibly extra info (off-site measurements, radar images, etc.)

- Their importance varies as a function of the lead time of interest...

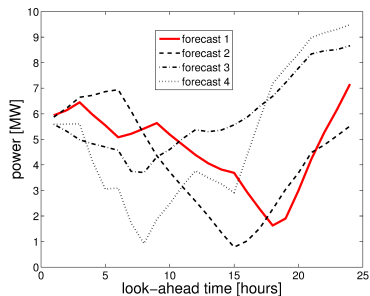
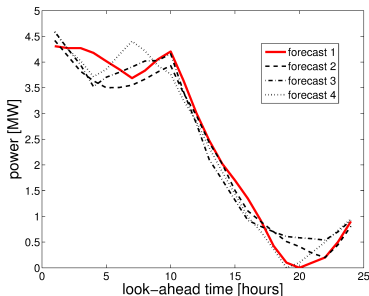
- *short-term* (0-6 hours): you definitely need measurements
- *early medium-range* (6-96 hours): weather forecasts are a must have!



- Future values of meteorological variables (wind, temperature, etc.) on a grid
- Temporal/spatial resolution, domain, forecast update and forecast length vary depending upon the NWP system
- Large number of alternative system today (global, mesoscale, etc.) providing free or commercially available output.
- **Origins of uncertainty in NWP:** initial state, model/physics, numerical aspects (filtering)



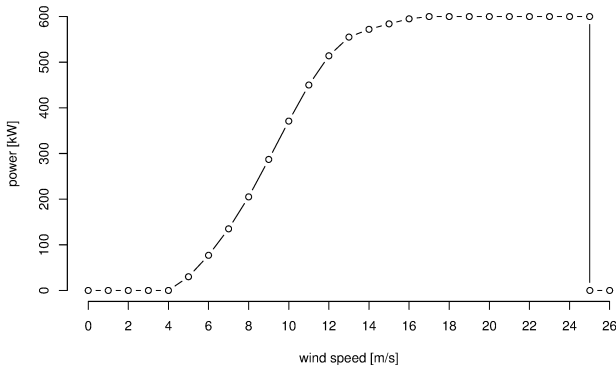
- A large part of the prediction error directly comes from prediction of weather variables
- This uncertainty in the meteorological forecast is then amplified or dampened by the power curve (model)



*Typical representation of what could be more and less easily predictable situations...*

## The manufacturer power curve

- Power curve of the Vestas V44 turbine (600 kW)

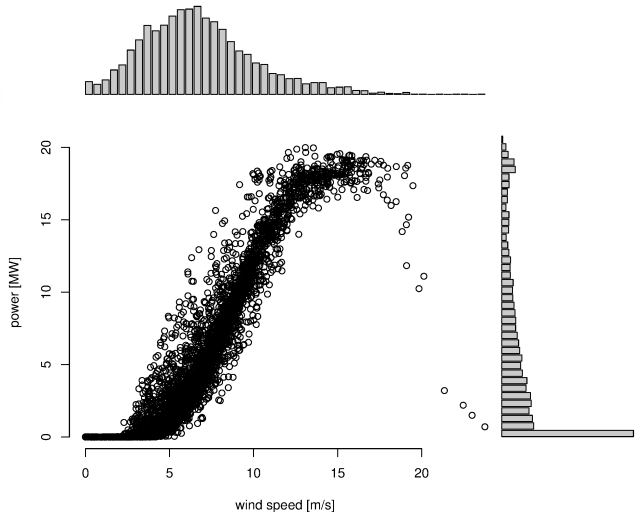


- **Klim wind farm** (North of Jutland, Denmark): 35 V44 turbines
- **Nominal capacity:** 21 MW
- Straightforward scaling of the power curve from 600kW to 21MW!

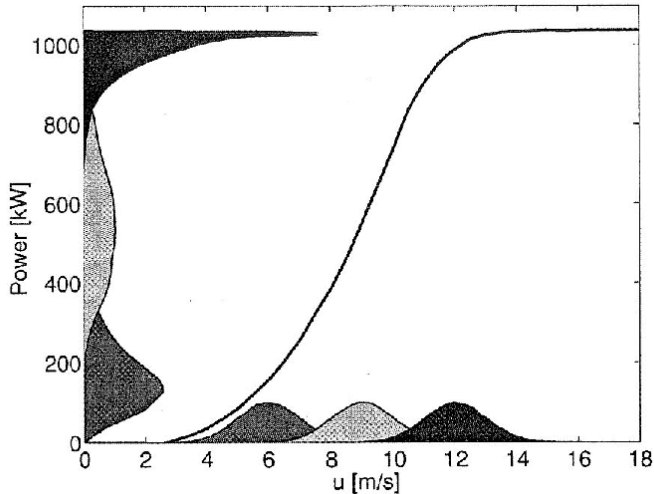
## The *actual* power curve looks different!

### Origins of uncertainty in the conversion process:

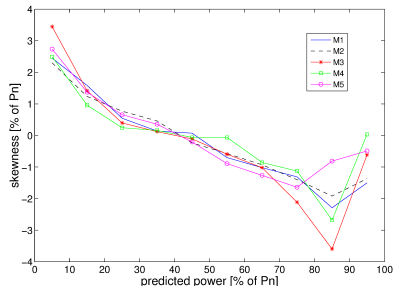
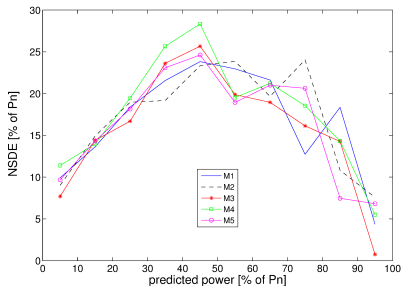
- actual meteorological conditions seen by turbines,
- aggregation of individual curves,
- non-ideal power curves,
- etc.



*courtesy of Matthias Lange*



### The power curve of a wind farm shapes the distributions of prediction errors



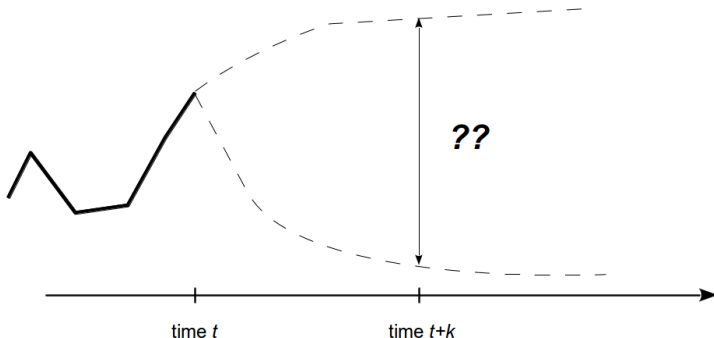
*the above example involves 5 different approaches to point prediction, for the same site, over the same period and with the same inputs...*

## 3 From deterministic to probabilistic forecasts

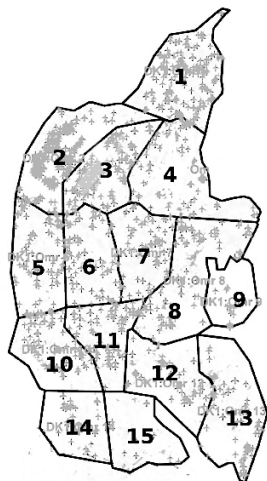


## Forecast setup: Forecasting is about the future!

- The practical setup:
  - we are at time  $t$  (e.g., at 11am, placing offers in the market)
  - and interested in what will happen at time  $t + k$  (any market time unit of tomorrow, e.g., 12-13)
  - $k$  is referred to as the **lead time**
  - $Y_{t+k}$ : the random variable “power generation at time  $t + k$ ”



- A forecast is an estimate for time  $t + k$ , conditional to information up to time  $t$ ...
- This motivates the notation  $\hat{\cdot}_{t+k|t}$



Agg. zone	Orig. zones	% of capacity
1	1, 2, 3	31
2	5, 6, 7	18
3	4, 8, 9	17
4	10, 11, 14, 15	23
5	12, 13	10

**Figure:** The Western Denmark dataset: original locations for which measurements are available, 15 control zones defined by Energinet, as well as the 5 aggregated zones, for a nominal capacity of around 2.5 GW.

**A point forecast informs of the conditional expectation of power generation**

Mathematically:

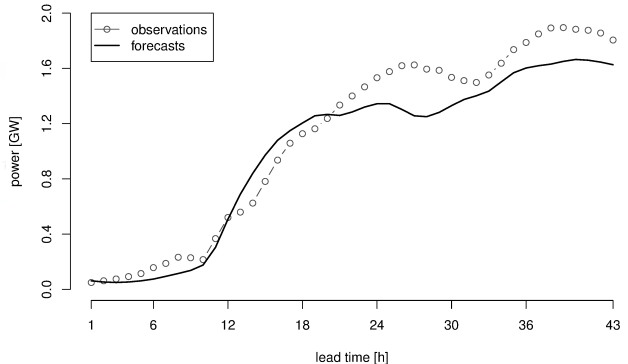
$$\hat{y}_{t+k|t} = \mathbb{E}[Y_{t+k} | \Omega, M, \hat{\theta}]$$

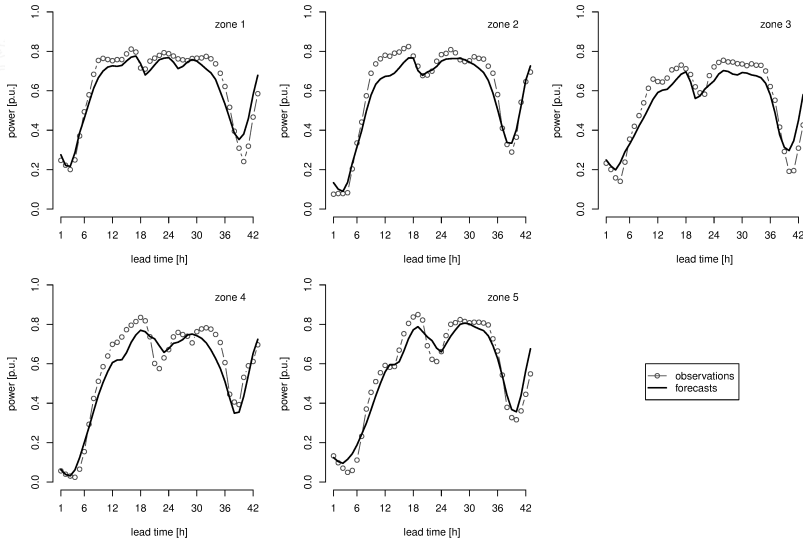
given

- the information set  $\Omega$
- a model  $M$
- its estimated parameters  $\hat{\theta}$

at time  $t$

*( $\Omega, M, \hat{\theta}$  omitted in other definitions)*





**Figure:** Example episode with point forecasts for the 5 aggregated zones of Western Denmark, as issued on 16 March 2007 at 06 UTC, along with corresponding power measurements, obtained a posteriori.

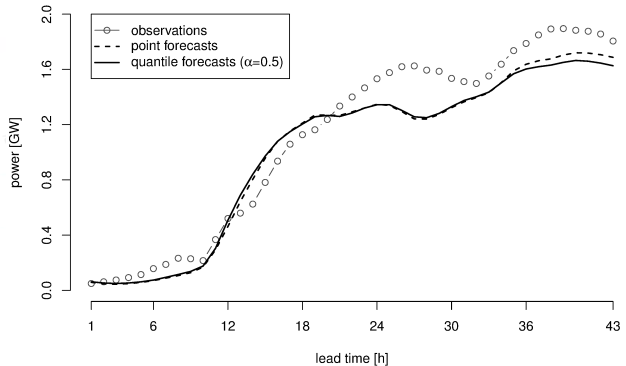
A quantile forecast is to be seen as a probabilistic threshold for power generation

Mathematically:

$$\hat{q}_{t+k|t}^{(\alpha)} = \hat{F}_{t+k|t}^{-1}(\alpha)$$

with

- $\alpha$ : the nominal level (ex: 0.5 for 50%)
- $\hat{F}$ : (predicted) cumulative distribution function for  $Y_{t+k}$



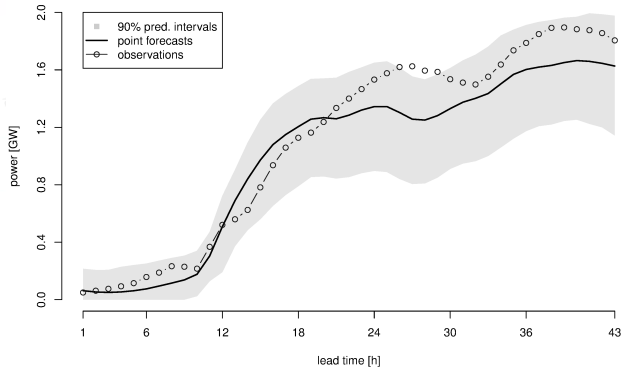
A prediction interval is an interval within which power generation may lie, with a certain probability

Mathematically:

$$\hat{l}_{t+k|t}^{(\beta)} = \left[ \hat{q}_{t+k|t}^{(\underline{\alpha})}, \hat{q}_{t+k|t}^{(\overline{\alpha})} \right]$$

with

- $\beta$ : nominal coverage rate (ex: 0.9 for 90%)
- $\hat{q}_{t+k|t}^{(\underline{\alpha})}, \hat{q}_{t+k|t}^{(\overline{\alpha})}$ : interval bounds
- $\underline{\alpha}, \overline{\alpha}$ : nominal levels of quantile forecasts



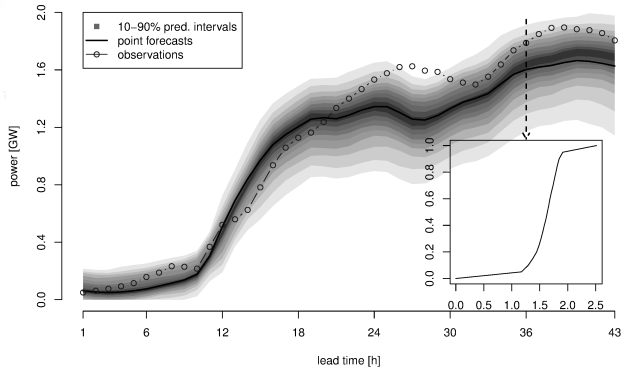
**A predictive density fully describes the probabilistic distribution of power generation for every lead time**

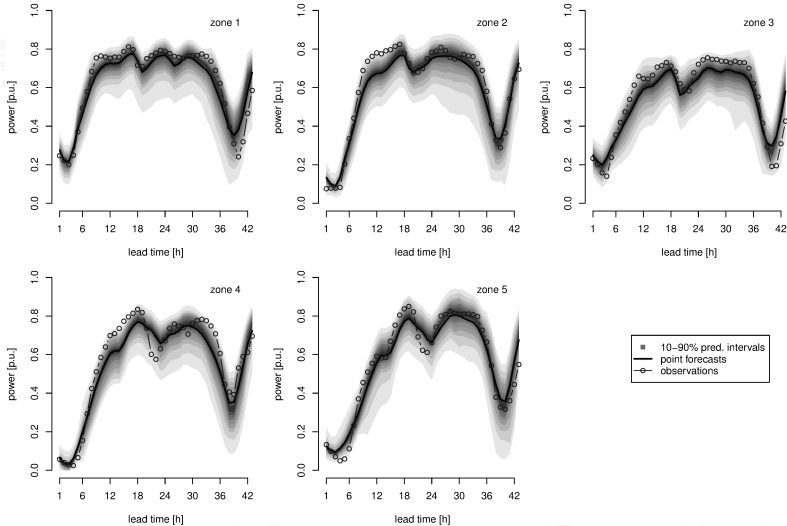
Mathematically:

$$Y_{t+k} \sim \hat{F}_{t+k|t}$$

with

- $\hat{F}_{t+k|t}$  :  
cumulative  
distribution  
function for  $Y_{t+k}$   
(predicted given  
information  
available at time  
 $t$ )



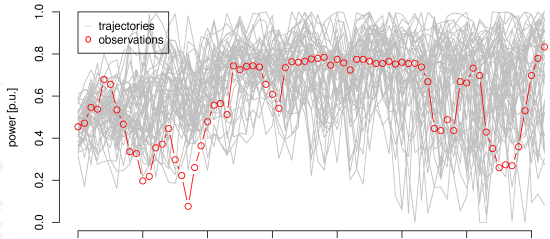


**Figure:** Example episode with probabilistic forecasts for the 5 aggregated zones of Western Denmark, as issued on 16 March 2007 at 06UTC. They take the form of so-called river-of-blood fan charts, represented by a set of central prediction intervals with increasing nominal coverage rates (from 10% to 90%).

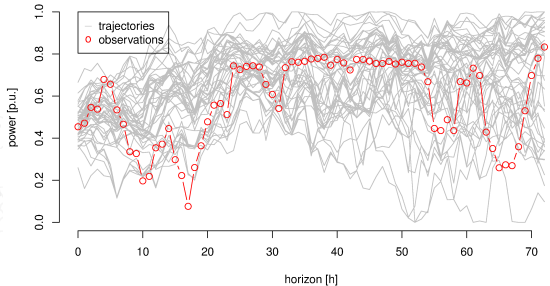


# The conditional importance of correlation

- almost no temporal correlation



- appropriate temporal correlation



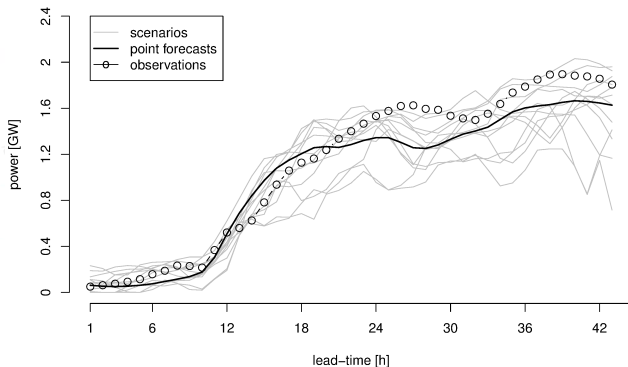
**Trajectories are equally-likely samples of multivariate predictive densities for power generation (in time and/or space)**

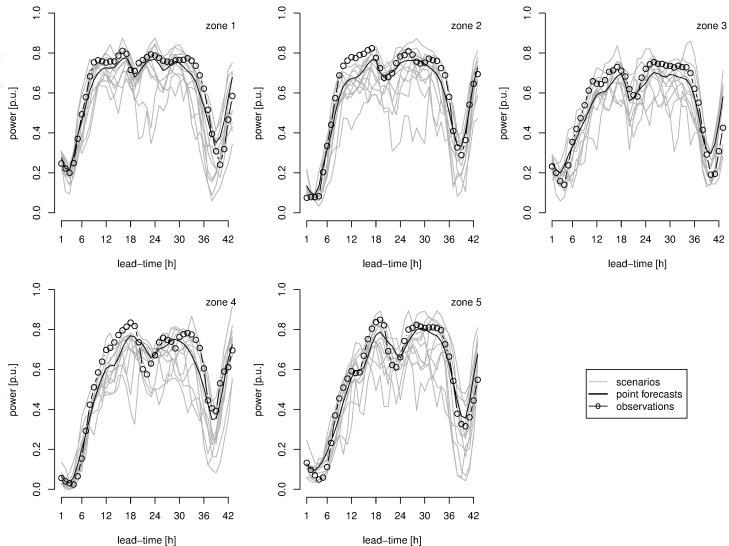
Mathematically:

$$z_t^{(j)} \sim \hat{F}_t$$

with

- $\hat{F}_t$ : multivariate predictive cdf for  $\mathbf{Y}_t$
- $z_t^{(j)}$ : the  $j^{\text{th}}$  trajectory





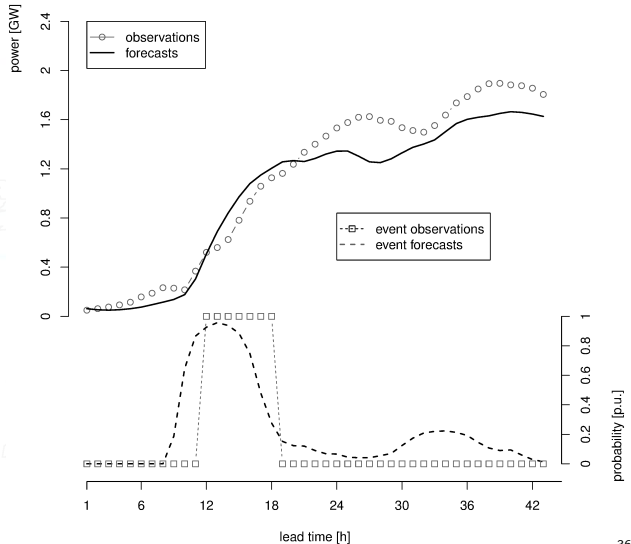
**Figure:** Spatio-temporal scenarios of wind power generation for the 5 aggregated zones of Western Denmark, issued on the 16 March 2007 at 06 UTC.

### Some decision-makers only want forecasts for user defined events

Examples are:

- ramp forecasts
- high-variability forecasts
- etc.

On the right: **probability of ramp forecasts (more than 500 MW swing in 6 hours)!**



- **Uncertainty is a key feature** of all renewable energy forecasts
- Lots of **different types of forecasts** inform of uncertainty, depending upon:
  - what they are to be used for
  - the expertise/feeling of the decision-maker
  - computing power available
- Approaches to characterizing, modelling and forecasting uncertainty in the following lectures...
- Before to generate forecasts, one should know how to verify(/evaluate) them!

Thanks for your attention! - Contact: [ppin@dtu.dk](mailto:ppin@dtu.dk) - web: [www.pierrepinson.com](http://www.pierrepinson.com)

