Literature

Competing first passage percolation on $\mathbb{Z}^d$

The model was introduced in [11], where it was also shown that two types with equal intensity can coexist in $d = 2$. This is generalized to higher dimensions (and more general passage time distributions) independently in [9] and [13]. A partial result concerning non-coexistence is proved in [12] and the full coexistence conjecture is proved in the half-plane in [2]. Further references can be found in the survey [7].

Competing first passage percolation on the configuration model

Exponential passage times are treated in [8] (power law with infinite variance), [3] (finite variance) and [4] (constant degrees). Constant passage times are treated in [6, 14].

Other models

A two-type version of the contact process was introduced in [19] and has been further studied in [17, 18, 21]. Other models for competition on $\mathbb{Z}^d$ include e.g. [1] (a combination of first passage percolation and bootstrap percolation), [15] (a model where sites can switch type) [16] (competition driven by random walks) and [20] (competing first passage percolation with mutation). A preferential attachment model with two types is analyzed in [5].

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